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# INVESTIGATING QUANTUM GRAPH VARIATIONS AS FUNCTIONS OF TIME

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## Abstract

The article deals with monotonically expanding and harmonic quantum star graphs featuring bonds of variable length. The study of these structures is important for processing particle transfer in various discrete structures, for instance, in quantum and molecular wire networks, as well as for carbon nanotubes and systems simulated by quantum graphs. We solved the Schrödinger equations for time-dependent graphs. We plotted and studied average kinetic energy as a function of time. We obtained spacetime diagrams of a Gaussian wave packet for the star graph.

## Keywords

Schrödinger equations, kinetic energy, discrete structures, quantum graph, boundary conditions

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